



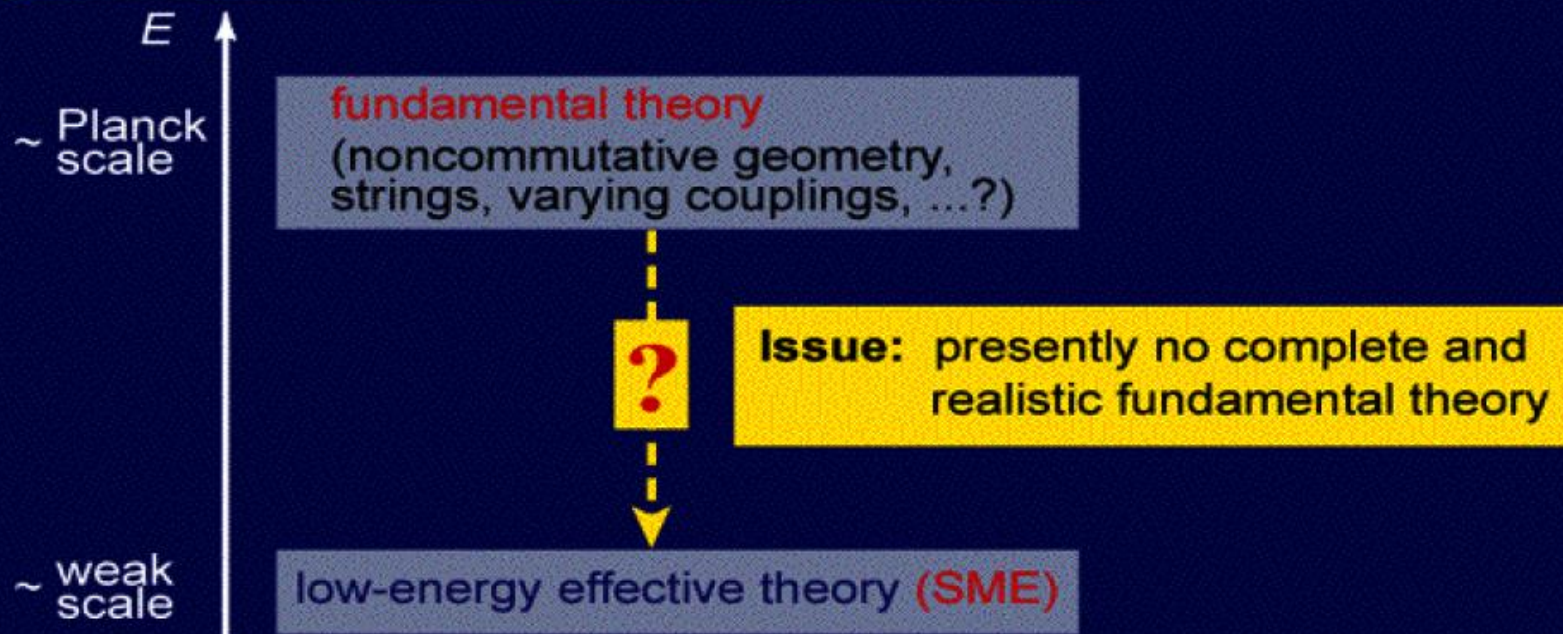
Results from $^3\text{He}/^{129}\text{Xe}$ clock comparison experiments for testing Lorentz invariance on the bound neutron

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Outline:

- Standard Model Extension (Kostelecky)
- ^3He , ^{129}Xe clock based on free nuclear spin precession
- New limits on LV from clock comparison experiments
- Conclusion and Outlook

How to obtain low-energy effective theory?



Idea:

- examine **manifestations** of Lorentz/CPT violating vacuum
- construct **all possible modifications** to SM (previous sec.)

Advantage:

- **independent** of underlying theory
- describes **all** low-energy effects of Lorentz violation

Standard-Model Extension

A. Kostelecky and C. Lane: **Phys. Rev. D 60, 116010 (1999)**

Modified Dirac equation for a free spin ½ particle (w=e,p,n)

$$\left(\underbrace{i\gamma^\mu \partial_\mu - m_w}_{\text{standard DE}} - \underbrace{a_\mu^w \gamma^\mu - b_\mu^w \gamma_5 \gamma^\mu + ie_v^w \partial^v - f_v^w \gamma_5 \partial^v + i \frac{1}{2} g_{\lambda\mu\nu}^w \sigma^{\lambda\mu} \partial^\nu}_{\text{CPT violating}} - \underbrace{\frac{1}{2} H_{\mu\nu}^w \sigma^{\mu\nu} + ic_{\mu\nu}^w \gamma^\mu \partial^\nu + id_{\mu\nu}^w \gamma_5 \gamma^\mu \partial^\nu}_{\text{CPT preserving terms}} \right) \Psi = 0$$

Lorentz violating terms

Experimental access:

$$a_\mu^w, b_\mu^w, \dots \approx \eta_w \cdot \left(\frac{m_w}{M_{Planck}} \right)^n$$

↑
coupling strength

Doppler-shift

Cs- fountain

Torsion pendulum

Antihydrogen spectroscopy

Astrophysics

Hg/Cs comparison

He/Xe maser

UCN/Hg comparison

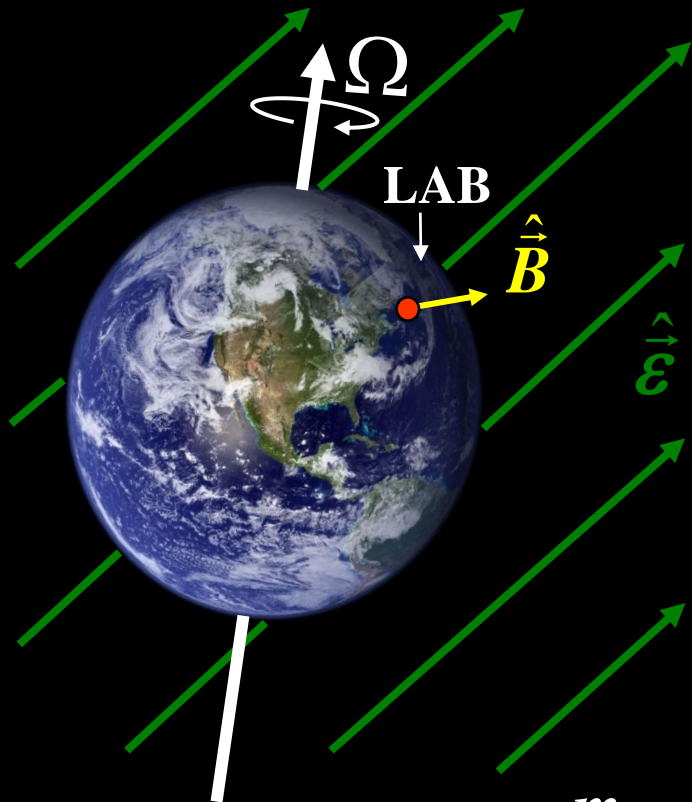
....

} clock
comparison
experiments

| Coefficient | Proton | Neutron | Electron | Coefficient | Proton | Neutron | Electron |
|---------------------------------|----------------|----------------|----------------|------------------------------------|----------------|----------------|----------------|
| \tilde{b}_X | 10^{-27} GeV | 10^{-31} GeV | 10^{-31} GeV | \tilde{H}_{XT} | – | 10^{-26} GeV | 10^{-27} GeV |
| \tilde{b}_Y | 10^{-27} GeV | 10^{-31} GeV | 10^{-31} GeV | \tilde{H}_{YT} | – | 10^{-27} GeV | 10^{-27} GeV |
| \tilde{b}_Z | – | – | 10^{-30} GeV | \tilde{H}_{ZT} | – | 10^{-27} GeV | 10^{-27} GeV |
| \tilde{b}_T | – | 10^{-27} GeV | 10^{-27} GeV | \tilde{g}_T | – | 10^{-27} GeV | 10^{-27} GeV |
| \tilde{b}_J ($J = X, Y, Z$) | – | – | – | \tilde{g}_c | – | 10^{-27} GeV | 10^{-27} GeV |
| \tilde{c}_- | 10^{-25} GeV | 10^{-27} GeV | 10^{-19} GeV | \tilde{g}_Q | – | – | – |
| \tilde{c}_Q | 10^{-22} GeV | – | 10^{-19} GeV | \tilde{g}_- | – | – | – |
| \tilde{c}_X | 10^{-25} GeV | 10^{-25} GeV | 10^{-19} GeV | \tilde{g}_{TJ} ($J = X, Y, Z$) | – | – | – |
| \tilde{c}_Y | 10^{-25} GeV | 10^{-25} GeV | 10^{-19} GeV | \tilde{g}_{XY} | – | – | – |
| \tilde{c}_Z | 10^{-24} GeV | 10^{-27} GeV | 10^{-19} GeV | \tilde{g}_{YX} | – | – | – |
| \tilde{c}_{TX} | 10^{-20} GeV | – | 10^{-18} GeV | \tilde{g}_{ZX} | – | – | – |
| \tilde{c}_{TY} | 10^{-20} GeV | – | 10^{-18} GeV | \tilde{g}_{XZ} | – | – | – |
| \tilde{c}_{TZ} | 10^{-21} GeV | – | 10^{-20} GeV | \tilde{g}_{YZ} | – | – | – |
| \tilde{c}_{TT} | – | – | 10^{-18} GeV | \tilde{g}_{ZY} | – | – | – |
| \tilde{d}_+ | – | 10^{-27} GeV | 10^{-27} GeV | \tilde{g}_{DX} | 10^{-25} GeV | 10^{-29} GeV | 10^{-22} GeV |
| \tilde{d}_- | – | 10^{-27} GeV | 10^{-27} GeV | \tilde{g}_{DY} | 10^{-25} GeV | 10^{-28} GeV | 10^{-22} GeV |
| \tilde{d}_Q | – | 10^{-27} GeV | 10^{-27} GeV | \tilde{g}_{DZ} | – | – | – |
| \tilde{d}_{XY} | – | 10^{-27} GeV | 10^{-27} GeV | | | | |
| \tilde{d}_{YZ} | – | 10^{-26} GeV | 10^{-27} GeV | | | | |
| \tilde{d}_{ZX} | – | – | 10^{-26} GeV | | | | |
| \tilde{d}_X | 10^{-25} GeV | 10^{-29} GeV | 10^{-22} GeV | | | | |
| \tilde{d}_Y | 10^{-25} GeV | 10^{-28} GeV | 10^{-22} GeV | | | | |
| \tilde{d}_Z | – | – | 10^{-19} GeV | | | | |

**Clock-comparison
experiments**

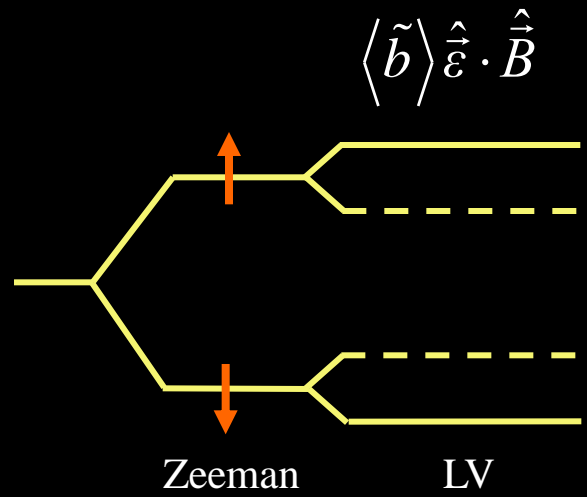
coupling of spin $\vec{\sigma}$ to background field: $V = -\vec{b} \cdot \vec{\sigma}$



$$H = -\vec{\mu} \cdot \vec{B} - \vec{b} \cdot \vec{\sigma}$$

$$\rightarrow \nu = \underbrace{\frac{2}{h} \mu B}_{\nu_{\text{Zeeman}}} + \underbrace{\frac{2}{h} \langle \tilde{b} \rangle \cos(\hat{e}, \hat{B})}_{\nu_{LV}}$$

natural scale: $\langle \tilde{b} \rangle \leq \frac{m_n}{M_P} \times m_n = 10^{-19} \text{ GeV}$



Clock-comparison:
Zeeman term drops out

$$\Delta\omega = \omega_A - \frac{\gamma_A}{\gamma_B} \omega_B = \left(1 - \frac{\gamma_A}{\gamma_B}\right) \cdot \omega_{LV}$$

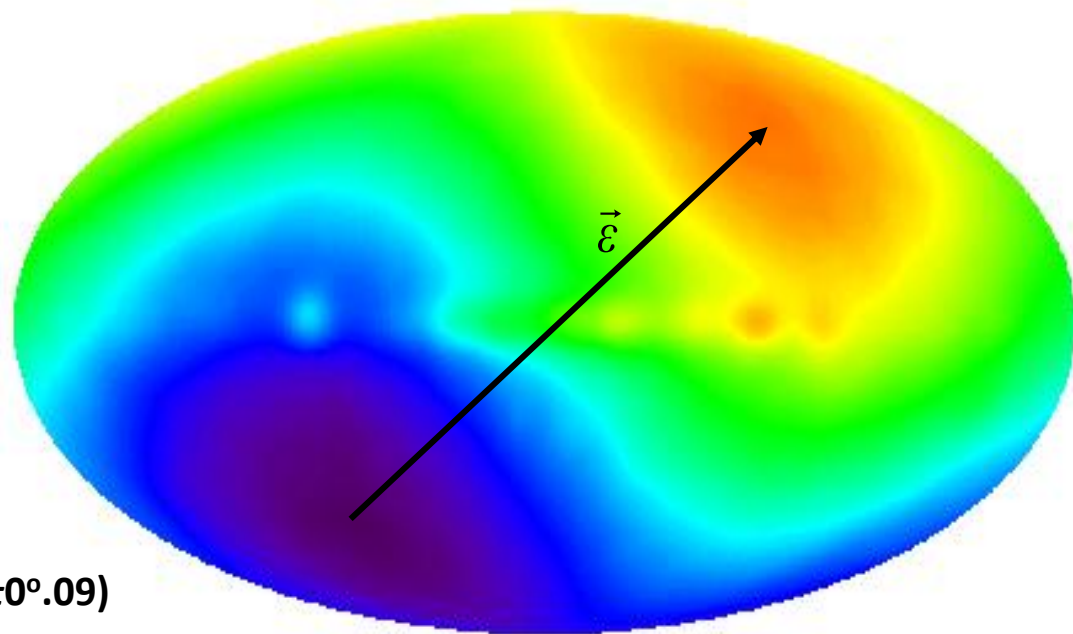
CMB dipole

$$v = 368 \text{ km/s}$$

$$\Delta T_{\text{dip}} \approx 3.3 \text{ mK}$$

galactic coordinate system

$$(l, b) = (264^\circ.31 \pm 0^\circ.04 \pm 0^\circ.16, +48^\circ.05 \pm 0^\circ.02 \pm 0^\circ.09)$$

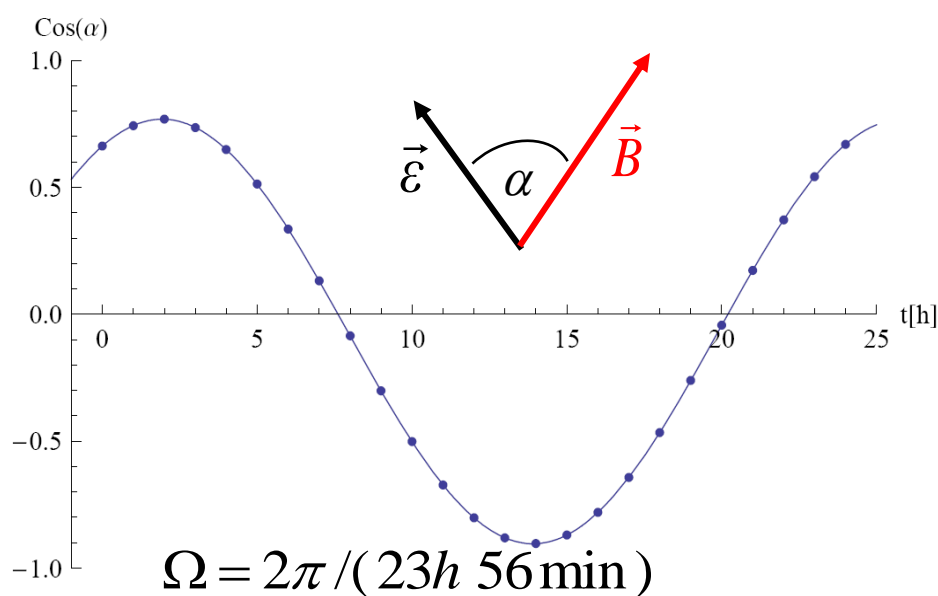
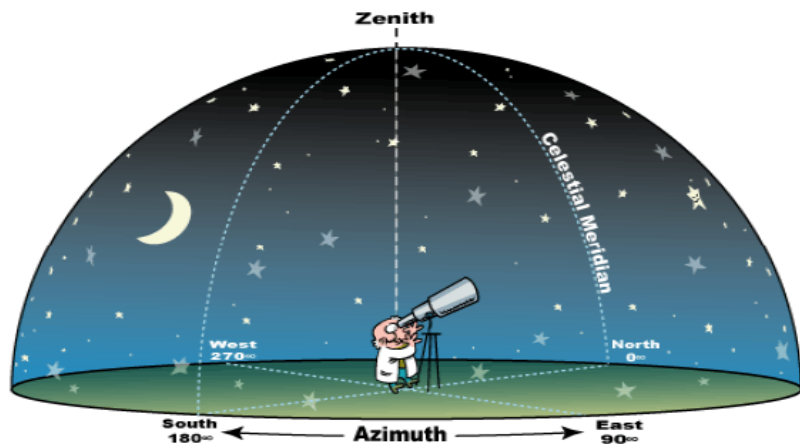


measurement on 01.10.2007 at

PTB-Berlin (52° 31' north, 13° 25' east)

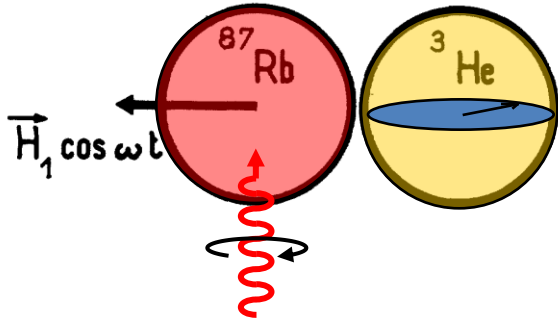
horizon coordinate system

(observer's local horizon)



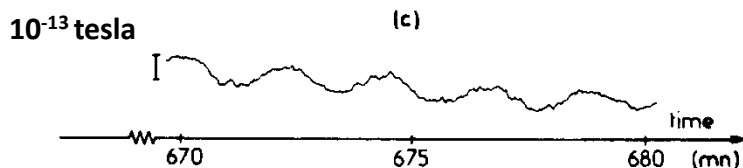
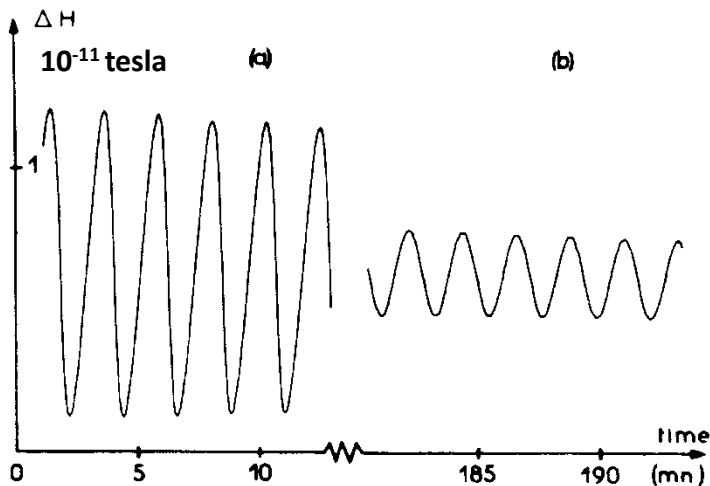
Detection of magnetic field produced by oriented nuclei

(Cohen-Tannoudji et al., PRL 22 (1969),758)



Results:

- ^3He spin precession: $T_2^* = 2\text{h } 20\text{min}$
- sensitivity of Rb-magnetometer:
100fT @ BW 0.3 Hz
- $P_{\text{He}} \approx 5\% @ 4\text{ mbar}$



Improvement of measurement sensitivity:

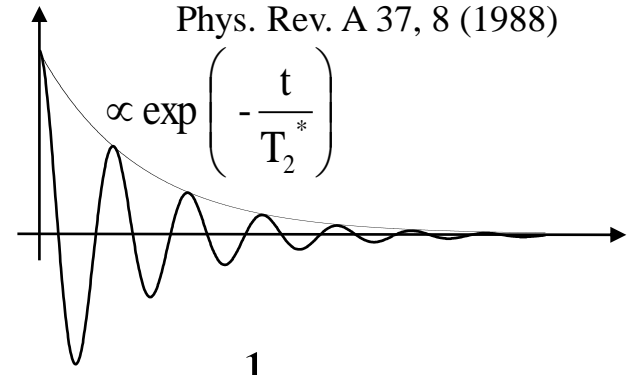
- SQUID-detectors @ 2 fT/ $\sqrt{\text{Hz}}$
- laser for OP of ^3He @ $P > 70\%$
- longer T_2^* -times (needed !!!)

Transverse Relaxation: T_2^*

Cates; Schaefer; Happer:
Phys. Rev. A 37, 8 (1988)

size: R
=> 3cm

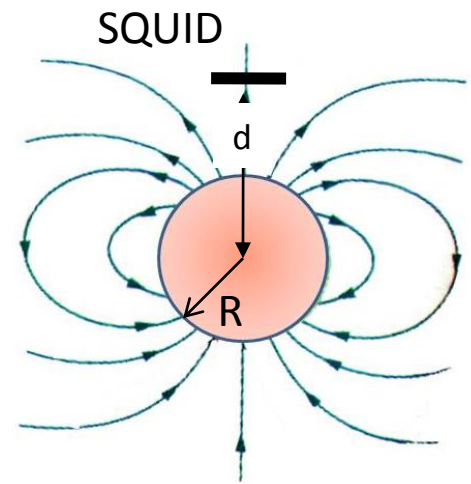
absolute gradient
→ low magn. field
($B_0 \approx 1 \mu\text{T}$)



$$\frac{1}{T_2^*} = \frac{1}{T_1} + \frac{8R^4 \gamma^2 |\vec{\nabla} B_{1z}|^2}{175D} + D \frac{|\vec{\nabla} B_{1x}|^2 + |\vec{\nabla} B_{1y}|^2}{B_o^2} \cdot \sum_n \frac{1}{|x_{1n}^2 - 2| \left[1 + x_{1n}^4 \left(\gamma B_o R^2 / D \right)^{-2} \right]}$$

longitudinal
relaxation time
 $T_1(\text{He}) > 100 \text{ h}$

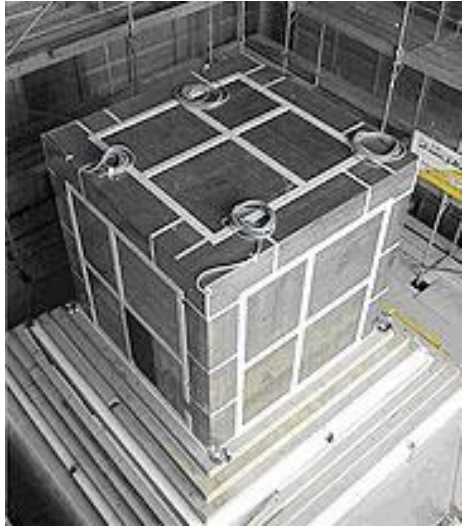
diffusion const. $D \sim 1/p$
→ low pressure
($p \sim \text{mbar}$)



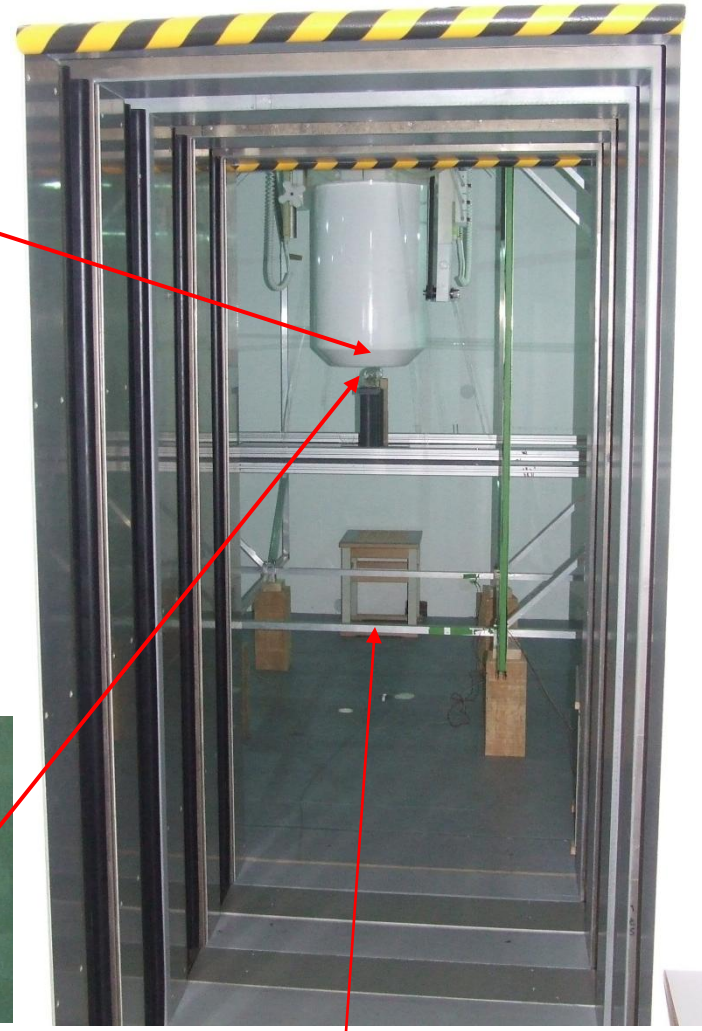
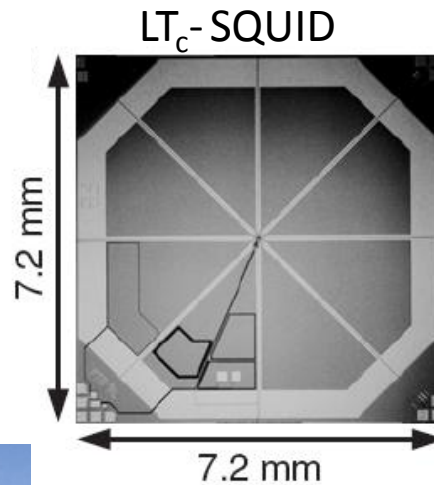
Signal:

$$\Delta B [pT] \approx 220 \cdot p [\text{mbar}] \cdot P \cdot \left(\frac{R}{d}\right)^3$$

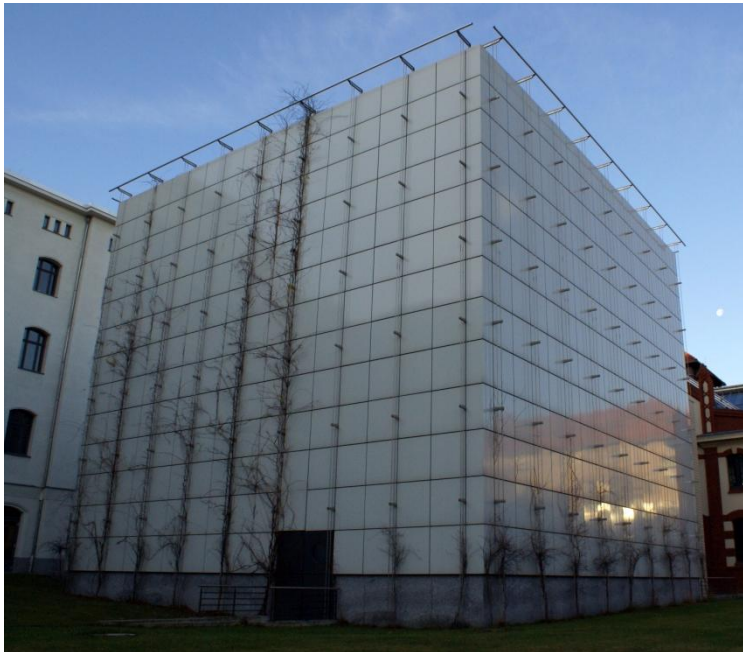
BMSR 2, PTB Berlin



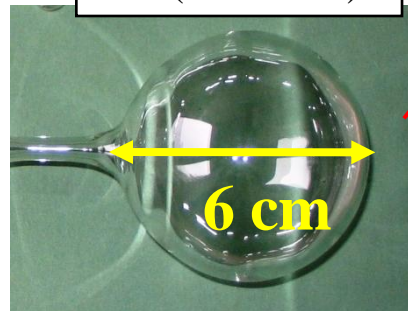
The 7-layered magnetically shielded room
(residual field < 2 nT)



J. Bork, et al., Proc. Biomag 2000, 970 (2000).



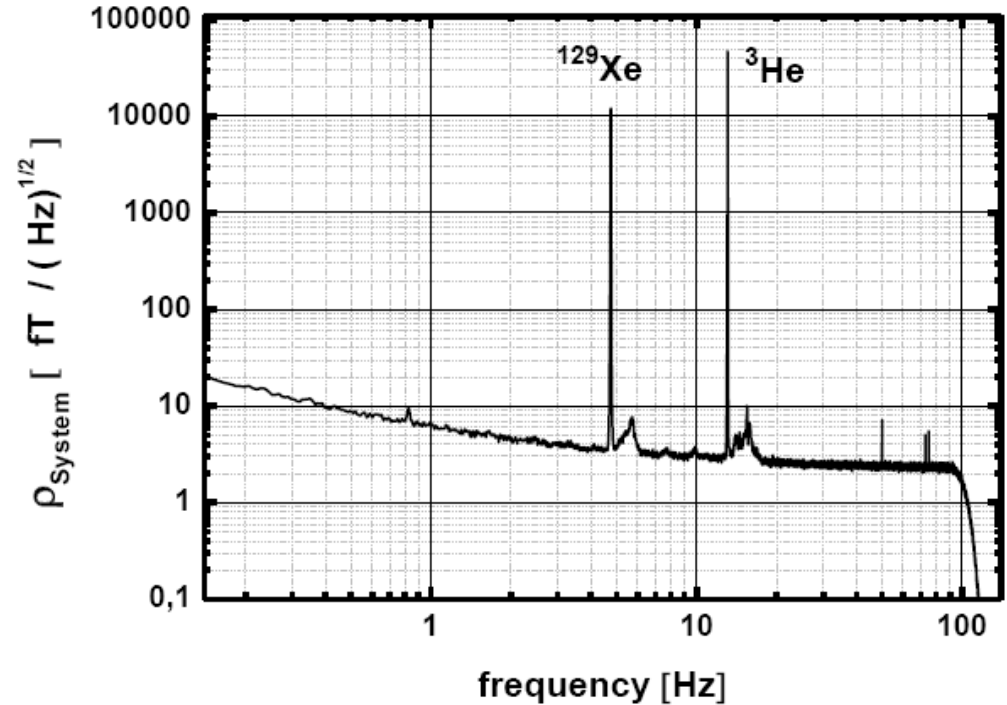
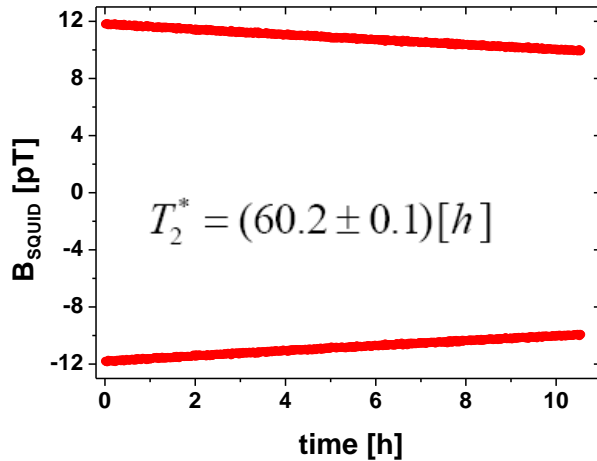
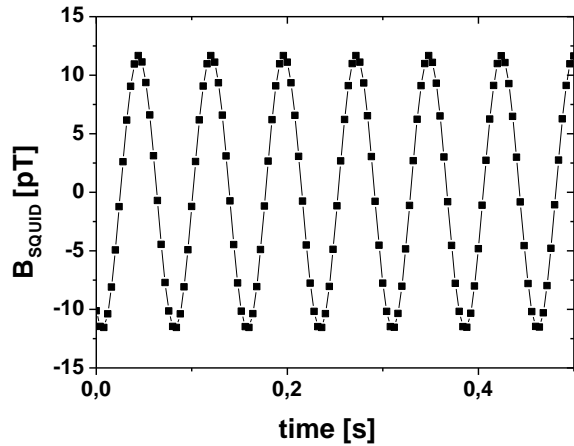
³He (4.5 mbar)



magnetic guiding field $\approx 0.4 \mu\text{T}$
(Helmholtz-coils)

$$\left| \vec{\nabla} B_{x,y,z} \right| \approx 20 \text{ pT} / \text{cm}$$

Sensitivity of a free spin-precession ^3He clock



Cramer-Rao Lower Bound (CRLB)

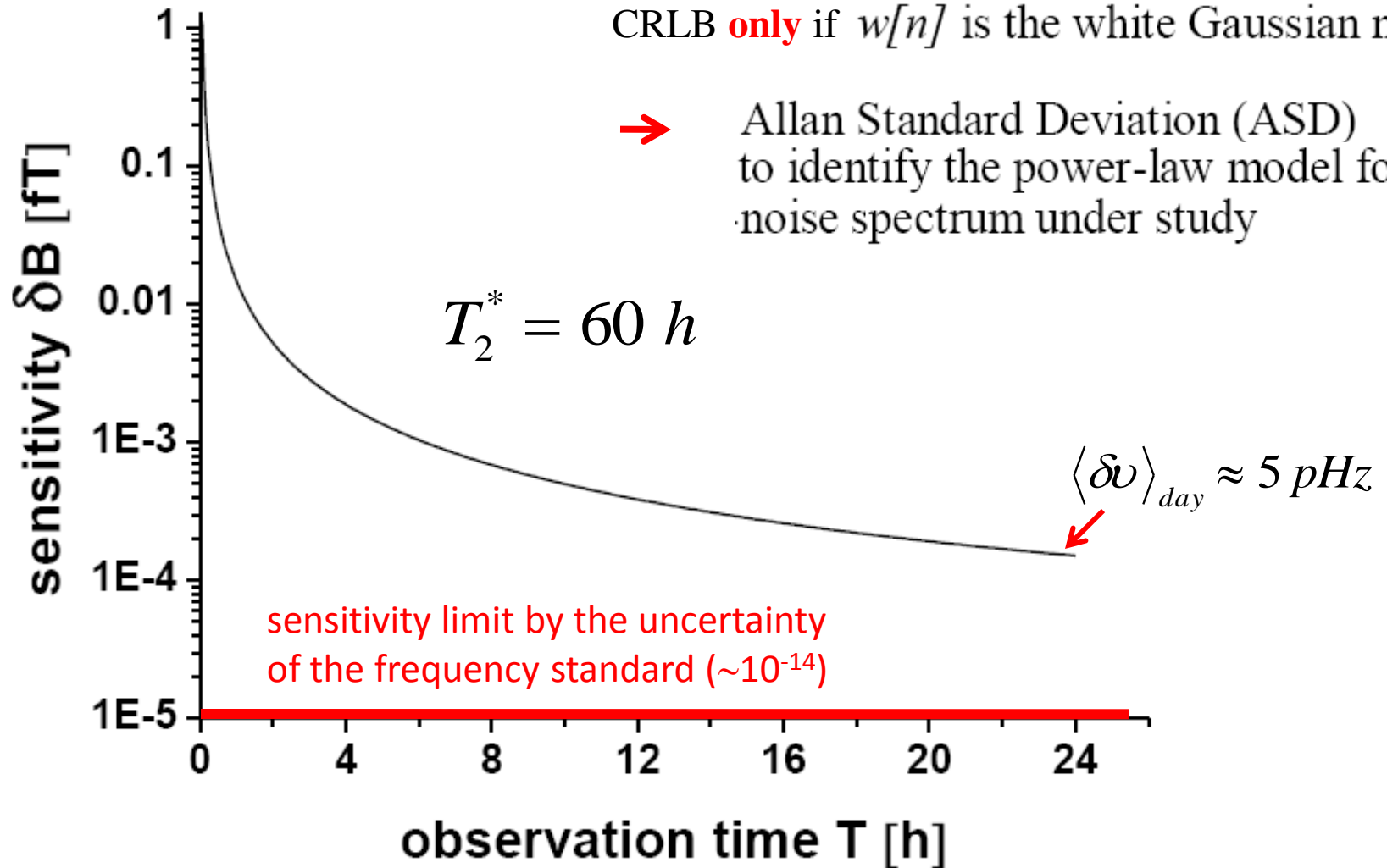
$$s[n] = A \cdot \cos(2\pi \cdot f \cdot \Delta t \cdot n + \Phi) \cdot \exp(-\beta \cdot n) + w[n] \quad n = 0, 1, 2, 3, \dots, N-1$$

$$\sigma_f^2 \geq \frac{12}{(2\pi)^2 (A / \rho_\alpha)^2 \cdot T^3} \cdot C$$

using $f = \gamma / (2\pi) \cdot B_0 \rightarrow \delta B [fT] \approx 3150 \cdot \frac{\sqrt{C}}{T^{3/2}}$

CRLB **only** if $w[n]$ is the white Gaussian noise

→ Allan Standard Deviation (ASD)
to identify the power-law model for the
noise spectrum under study

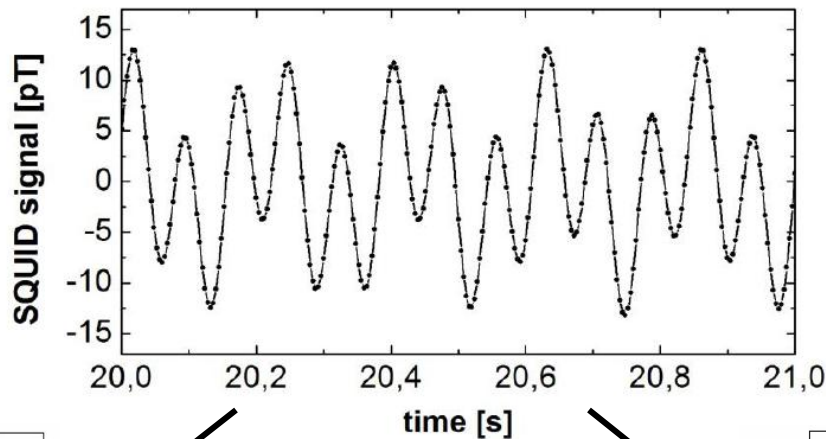
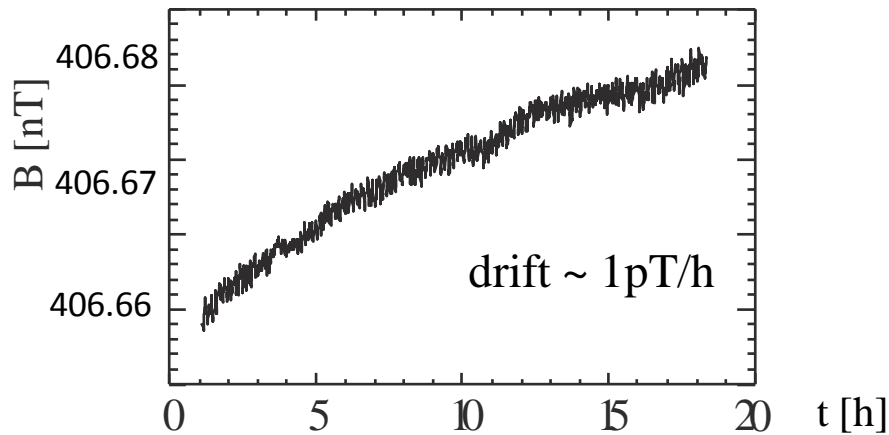
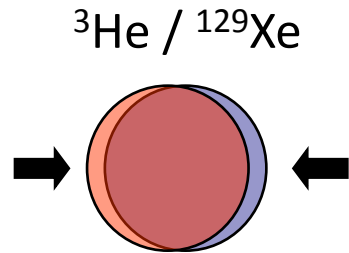


Advantage of long spin-coherence times:

$$\delta \nu \propto \frac{1}{T^{3/2}} \quad \text{vs. series of short } (\Delta T) \text{ measurements} \quad \delta \nu = \left(\frac{1}{\Delta T^{3/2}} \right) \cdot \frac{1}{\sqrt{T / \Delta T}} = \left(\frac{1}{T^{3/2}} \right) \cdot \frac{T}{\Delta T}$$

$^3\text{He} / ^{129}\text{Xe}$ co-magnetometer

variation of ω_{Zeeman} (field drifts)
much bigger than ω_{LV}

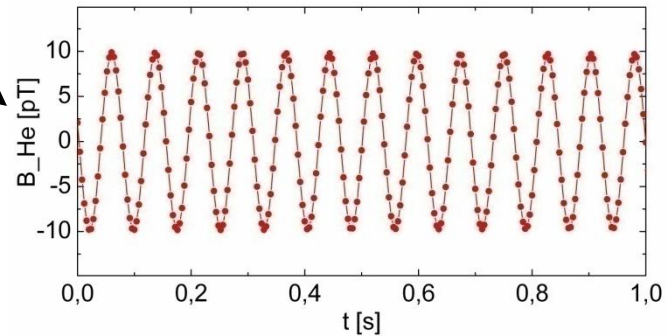
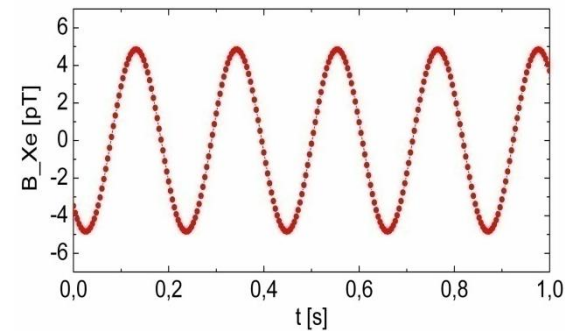


^{129}Xe

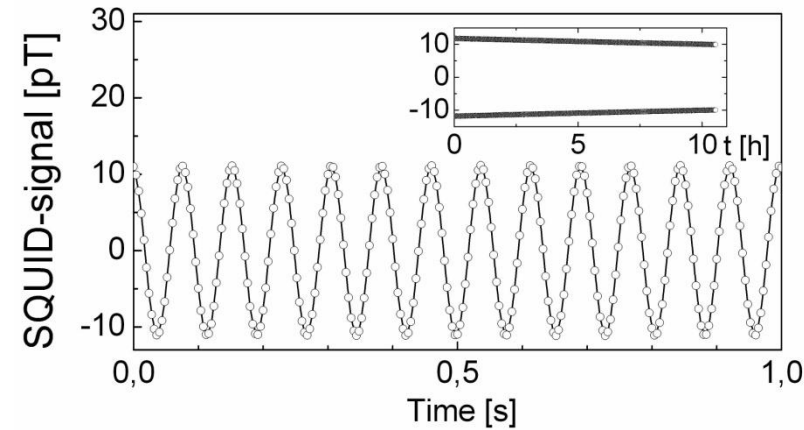
^3He

filtering:
4,7 Hz

filtering:
13 Hz



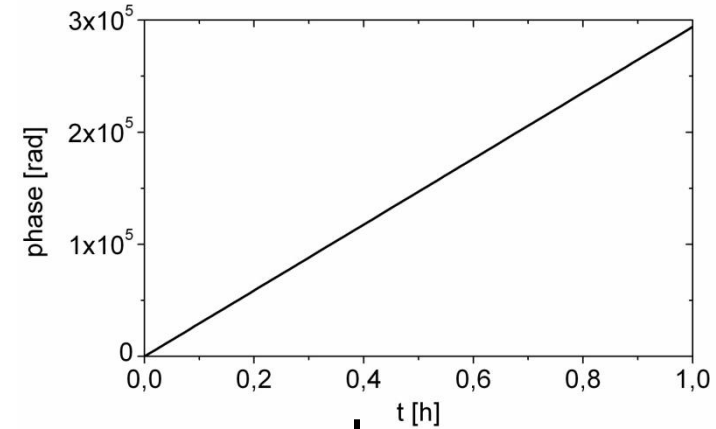
Analysis of phases



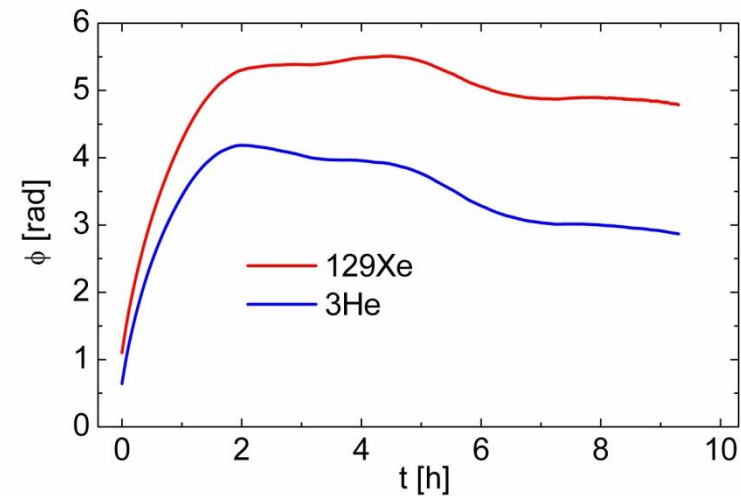
$$\Phi(t) = \int_0^t \omega(t') dt'$$

$$\omega(t) = \bar{\omega} + \Delta\omega(t)$$

($\Delta\omega \ll \bar{\omega}$)



subtract mean frequency: $\Phi'(t) = \int_0^t (\omega(t') - \bar{\omega}) dt'$

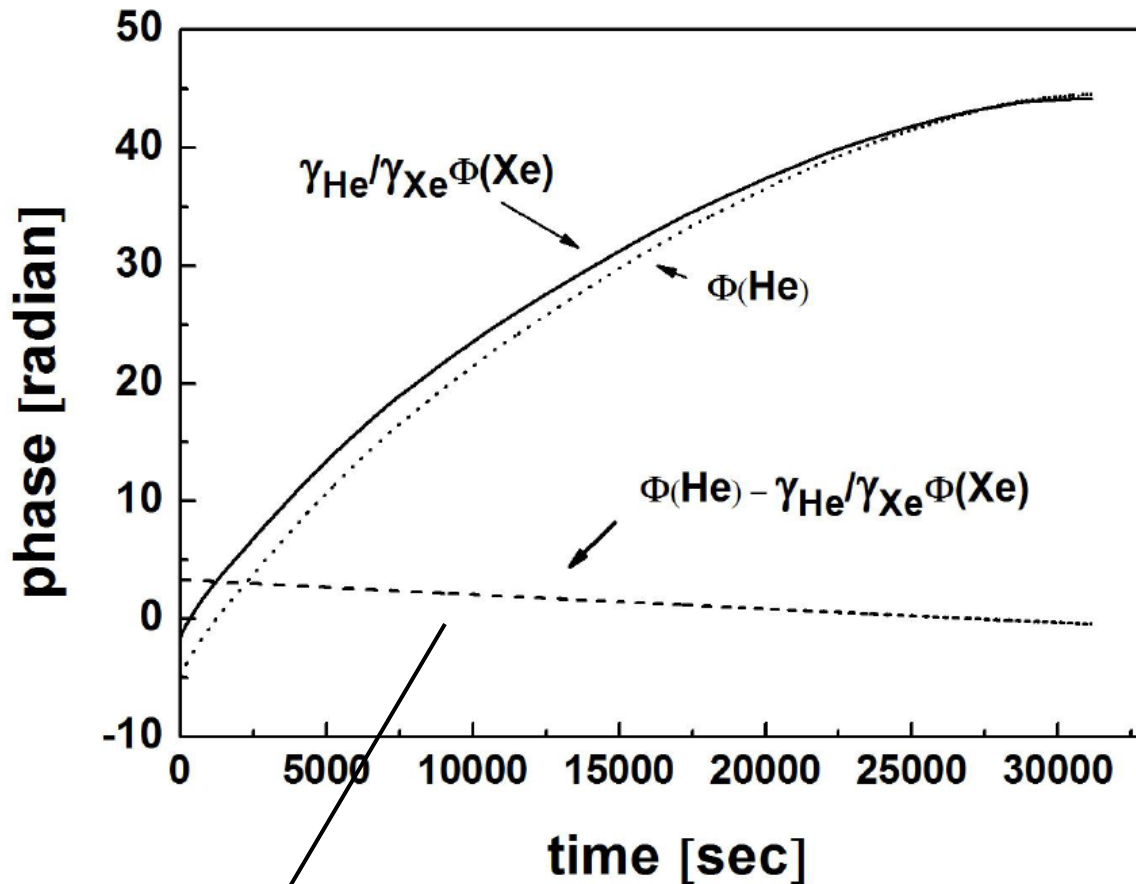


$$\gamma_{\text{He}} / \gamma_{\text{Xe}} = 2.75408159(20)$$

expected:

$$\Delta\Phi(t) = \Phi'_{\text{He}}(t) - \gamma_{\text{He}} / \gamma_{\text{Xe}} \cdot \Phi'_{\text{Xe}}(t)$$

$$= \Phi_0 + 2\pi / \Omega_s \cdot (\delta\nu_x \cdot \sin(\Omega_s t) - \delta\nu_y \cdot \cos(\Omega_s t))$$



Contribution to linear term:

- Earth's rotation

$$(1 - \gamma_{He}/\gamma_{Xe}) \cdot \frac{2\pi}{T_s} \cdot 0.544 \approx 0.069 \text{ mrad/s}$$

- chemical shift

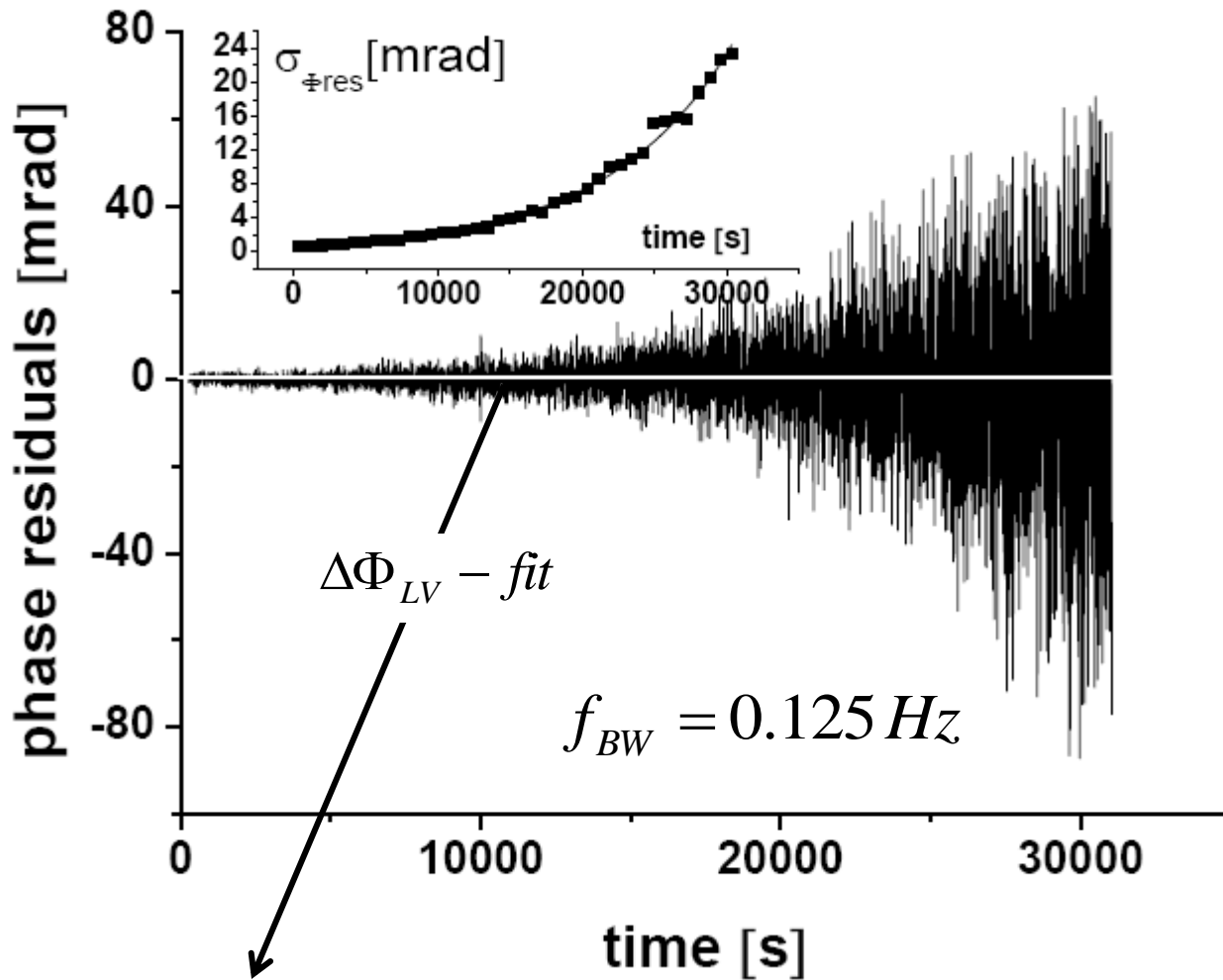
$$(\gamma_{He}/\gamma_{Xe})_{c.s.} \neq (\gamma_{He}/\gamma_{Xe})_{literature}$$

-

Exponential term:

$$20 \text{ h} < T_x < 70 \text{ h} \quad ?$$

$$\Delta\Phi = \Phi_0 + \Omega_L \cdot t + \Phi_1 \cdot \exp(-t/T_x) + \Delta\Phi_{LV}(t)$$



$$\delta\nu_x = (0.35 \pm 2.95) \cdot 10^{-9} \text{ Hz} \quad \text{and} \quad \delta\nu_y = (0.77 \pm 3.70) \cdot 10^{-9} \text{ Hz}$$

$$\Delta\nu_{\perp} = \sqrt{\delta\nu_x^2 + \delta\nu_y^2} = (0.8 \pm 4.7) \text{ nHz} \quad (67\% \text{ C.L.})$$

free neutron:

$$n: \mu = -1.913 \mu_K$$

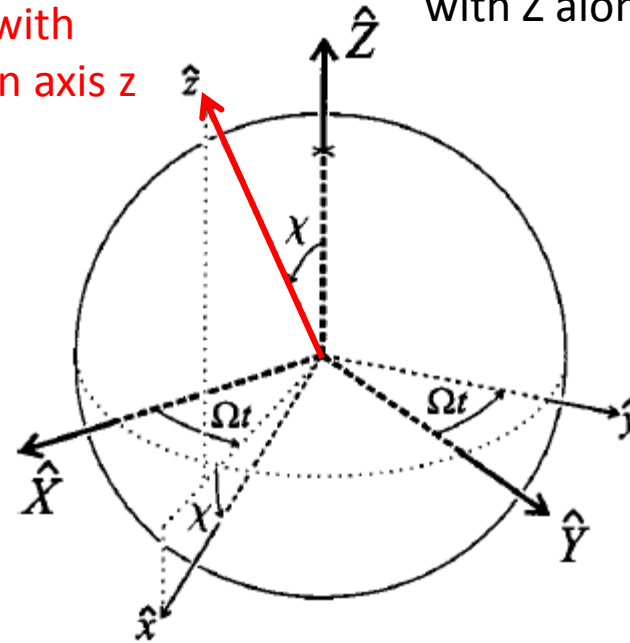
Schmidt-Model

$${}^3\text{He}: \mu = -2.1276 \mu_K$$

$${}^{129}\text{Xe}: \mu = -0.7779 \mu_K$$

Lab-frame with
quantization axis z

(X,Y,Z) non-rotating frame
with Z along Earth's rotation axis



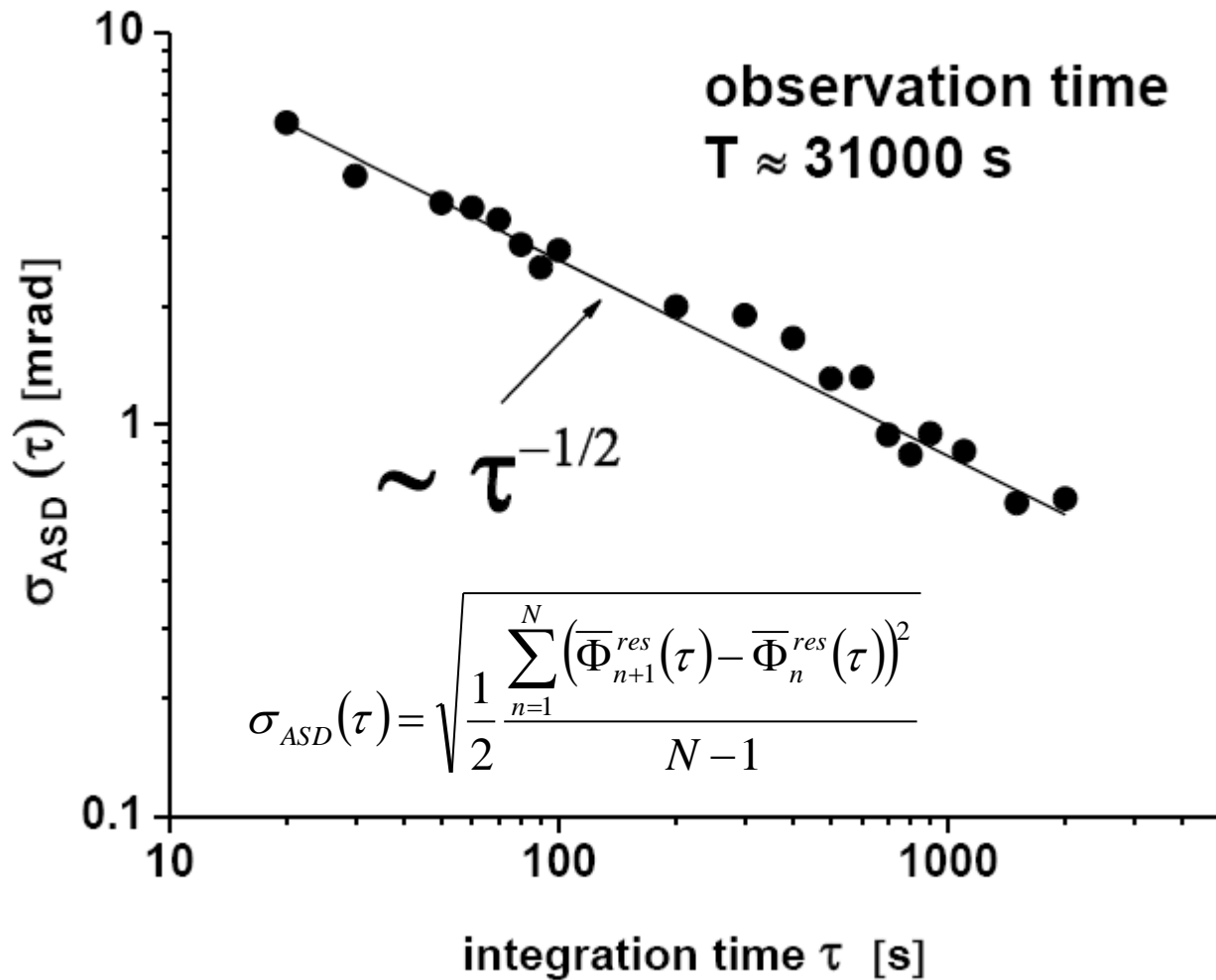
$$\begin{aligned} \cos \chi &= \cos \theta \cdot \cos \rho \\ &= 0.543 \end{aligned}$$

$$\begin{aligned} \theta &= 52^{\circ}31' \\ \rho &= 28^{\circ} \end{aligned}$$

$$\sin \chi \cdot \left| -3.5 \cdot \tilde{b}_J^n + 0.012 \cdot \tilde{d}_J^n + 0.012 \cdot \tilde{g}_{D,J}^n \right| \leq 2\pi \cdot \delta\nu_J \cdot \hbar \quad J = X, Y$$

$$\tilde{b}_{\perp}^n = \sqrt{(\tilde{b}_X^n)^2 + (\tilde{b}_Y^n)^2} \leq 7 \cdot 10^{-33} \text{ GeV}$$

ASD of residual phase noise

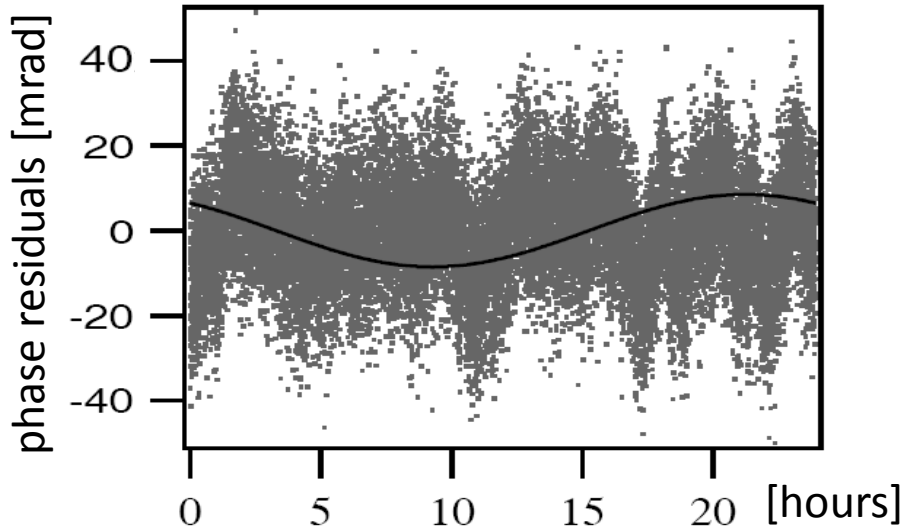
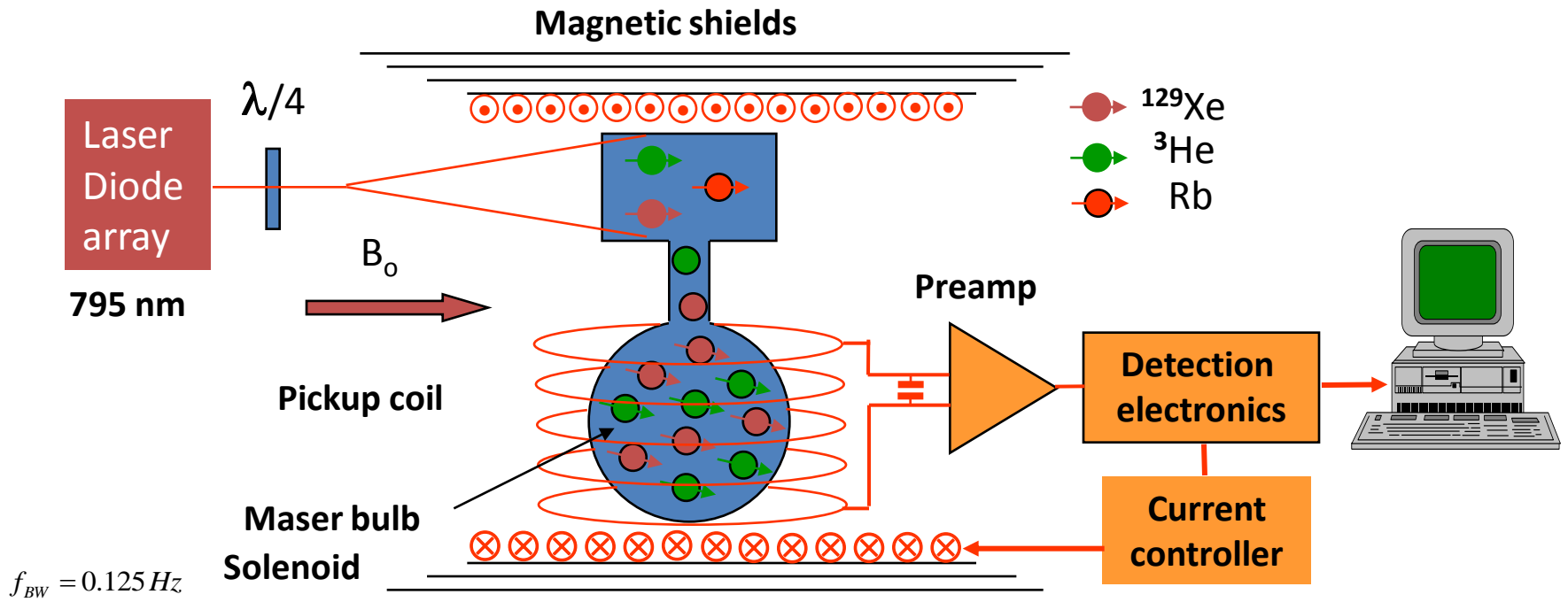


observed fluctuations decrease as $\tau^{-1/2}$ indicating the presence of a white phase noise

CRLB power law ✓

Spin maser experiments with ^3He and ^{129}Xe set the best limit on LV effects for the neutron

(D.Bear et al., PRL 85 (2000) 5038)



Fit to their data

$$\delta\phi = 2\pi \cdot \Omega_s^{-1} \left[\delta\nu_X \cdot \sin(\Omega_s t) - \delta\nu_Y \cdot \cos(\Omega_s t) \right]$$

$$\Rightarrow 2\pi |\delta\nu_J| \geq \frac{1}{\hbar} \cdot \left| -3.5 \tilde{b}_J^n \right|$$

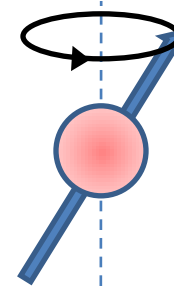
$$\Rightarrow \left| \tilde{b}_{X,Y}^n \right| < 10^{-31} \text{ GeV}$$

Conclusion and Outlook

- ^3He , ^{129}Xe clocks based on free spin precession
→ long spin coherence times

$$T_{2,\text{He}}^* > 60 \text{ hours}$$

$$T_{2,\text{Xe}}^* = 3 - 6 \text{ hours} \quad (\text{so far limited by } T_{1,\text{wall}})$$



- Magnetometry

$\langle \delta B \rangle \approx 1 \text{ fT} @ 200 \text{ s} \longrightarrow$ magnetometer for nEDM experiments

$$\langle \delta B \rangle \approx 10^{-4} \text{ fT} @ 1 \text{ day}$$

- clock comparison

$$\text{SME (Kostelecky):} \quad V = -\tilde{\vec{b}} \cdot \vec{\sigma}$$

new limits on the bound neutron

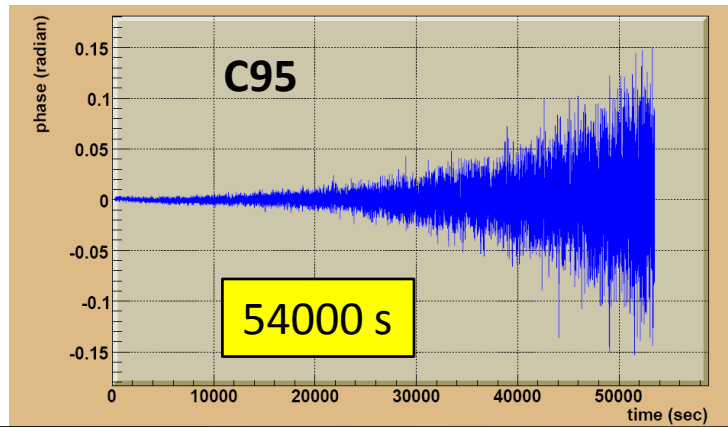
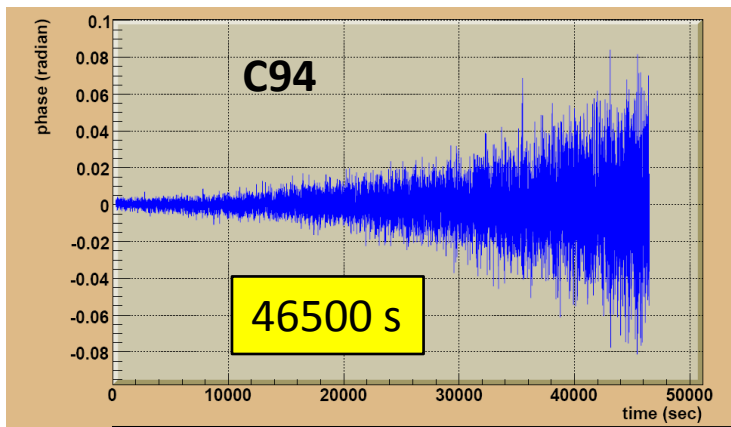
| Coefficient | Proton | Neutron | Electron |
|---------------|------------------------|------------------------|------------------------|
| \tilde{b}_X | 10^{-27} GeV | 10^{-31} GeV | 10^{-31} GeV |
| \tilde{b}_Y | 10^{-27} GeV | 10^{-31} GeV | 10^{-31} GeV |
| \tilde{b}_Z | – | – | 10^{-30} GeV |
| \tilde{b}_T | – | 10^{-27} GeV | 10^{-27} GeV |

$$|\tilde{b}_X^n| \leq 4 \cdot 10^{-33} \text{ GeV}$$

$$|\tilde{b}_Y^n| \leq 5 \cdot 10^{-33} \text{ GeV}$$

C.Gemmel et al., arXiv:0905.3677
submitted to EPJ D

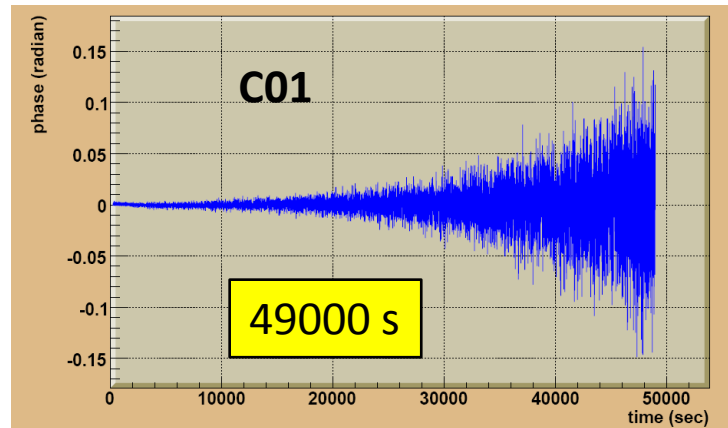
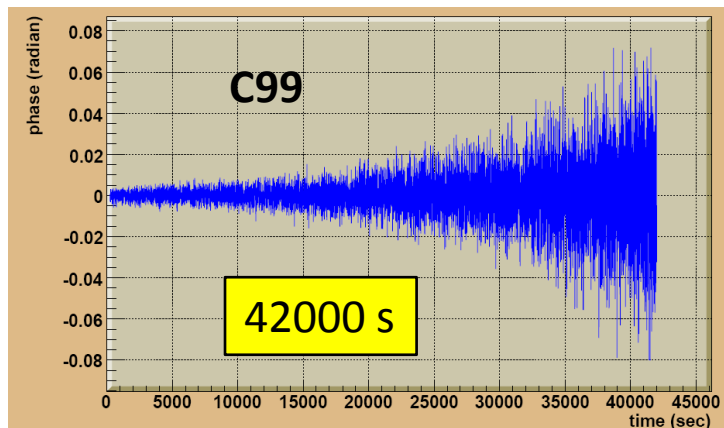
improved sensitivity: March 2009 run



[h]

0

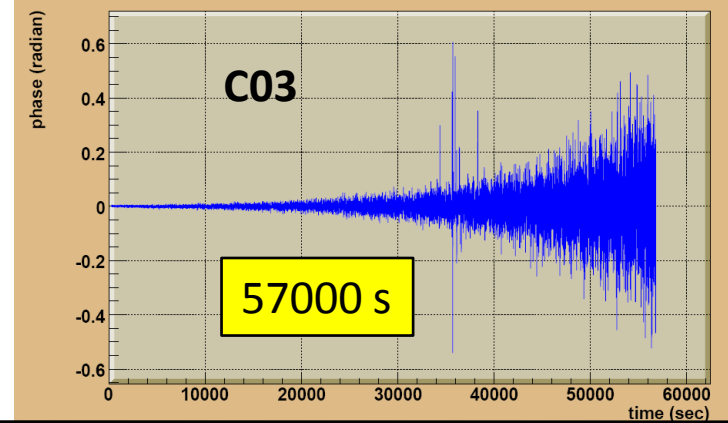
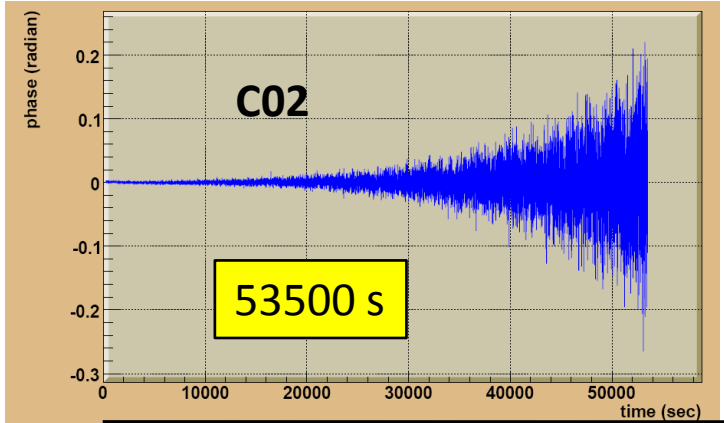
13:35



[h]

29:30

46:00



[h]

60:10

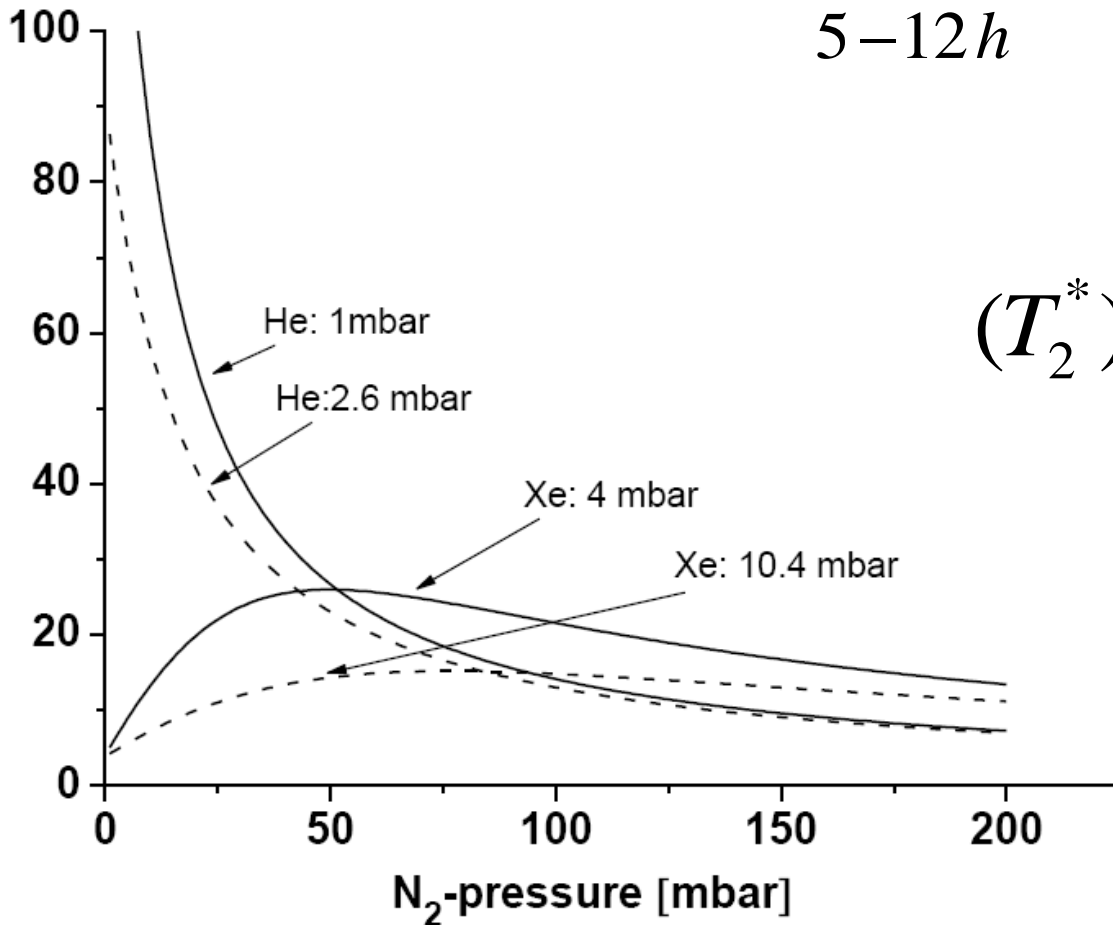
77:50

Relaxation of ^{129}Xe

$$\frac{1}{T_2^*} = \frac{1}{T_{1,\text{wall}}} + \frac{1}{T_{1,\text{vdW}}} + \frac{1}{T_{2,\text{field}}}$$

\swarrow \searrow
 $5-12h$ $\frac{1}{4.1h} \cdot \frac{1}{(1+1.05 \cdot [N_2]/[Xe])}$

$$\left(\frac{1}{T_{1,\text{vdW}}} + \frac{1}{T_{2,\text{field}}} \right)^{-1} [h]$$



$$(T_2^*)_{\text{Xe}} \approx 3-6h$$

(measured)